## Stability Analysis Of 7<sup>1</sup>/<sub>2</sub> Inch Gauge Ride-On Trains

### Introduction

Large scale trains operating on 7 1/2" (or 7 1/4" in some areas) gauge track have operated safely for many thousands of miles carrying passengers of all types. They have an amazing ability to accommodate persons of varying ages, many sizes, and those with disabilities. We are all familiar with clubs that offer rides to persons beyond the immediate friends and family of the club member or equipment owner. The public service record of providing a fun, safe day to scout troops, cancer survivors, and birthday parties is one of he outstanding merits of being involved in the operation of these trains.

### History

For many years small amusement ride operations used train equipment approximately onequarter full size, most commonly on 15 inch gauge track. This size of equipment was very stable and dependable for commercial operations. It required a great deal of space for track and storage, was heavy to transport if moved, and was unaffordable to many individual hobbyists.

With time a new size based on dividing 15 inch gauge in half resulted in the 7 1/2" gauge equipment that is so common today. This also made possible larger size, more complex, and more detailed models as individual preferences developed. The smaller scale made possible home layouts, and models that could be taken from home to home or to clubs.

### Ridership

In years past the common approach to a club or private track offering rides was that it was understood that the builder, owner, and operator were all amateurs. They did not do any of these things for a living, were not an expert, and were offering to do the best they could in providing a safe experience in riding a model train.

In the past few years some operators seem to have moved away from this view. Perhaps it is the desire to appear professional in what we do. For some clubs that are on public land it is a pressure from outside to provide more rides with less restrictions on who can ride. In a few cases it was motivated by an ability to collect money, either as a fare or as a donation, for providing the rides.

We really don't like to say it but we are more and more living in a society in which any problem ends up in the legal system. If you are offering rides to persons that feel they are being transported by a system equivalent to a commercial amusement park, they are more likely to demand significant attention if anything goes wrong.

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The combined pressures of carrying persons who, in the past, may not have been allowed to ride, and the likelihood of serious legal, insurance, and financial issues if there is an accident, combine to make many persons reluctant to participate. However, if this is carried to extreme the clubs and tracks we all need to enjoy our equipment will disappear. It is admittedly a pleasure to operate your locomotive with a good load to pull. And hopefully the pleasure provided to the passengers will also bring you joy. So we need to look carefully at the equipment we operate and understand the limitations in what it can and cannot do for us.

## **Background and Terminology**

This document focuses on equipment operating on 7 1/2" gauge track. In the case of 7 1/4" gauge the results would be very similar and the work done here has not been repeated for this other size. The information presented applies to any scale (1 1/2, 1.6, 2 1/2, etc.) that operates on this gauge track. For smaller scales and narrower gauges it is certain that most persons operating this equipment understand that they are very limited in who they can allow to ride because of the lesser stability. In looking at larger gauges, 9" is somewhat more stable than the results shown here. Still larger gauges, 12" and above, benefit greatly from the combination of wider wheel spacing and much heavier cars. Once we get to 15" gauge we are in the range of commercial operations that can safely operate with a wide range of passenger types.

### **Defining Stability**

In looking at how to transport a passenger safely we must consider three components, the passenger, the car, and the track. This assumes that the car includes any seating, supports, footrests, etc. as a rigid part of the car.

For passengers we will simplify all the possible shapes and sizes to simply consider their weight (mass) concentrated a single point.

This reduces our stability analysis to what is shown in Figure 1. While the track gauge is 7 1/2", the actual point of contact between the wheels and rails is somewhat wider. We have simplified our analysis by assuming this distance is 8".

We can define stability as positive, neutral, and negative. We have selected the point of contact between the left side wheel and left rail as a point about which all of our calculations will pivot. This means that positive stability is when there is some amount of downward force on the right side wheel to rail contact. While actual operation will require this to be at least a moderate amount for this analysis we will assume positive stability with any amount of force here at all.

Neutral stability is then when the force between the right side wheel and rail is zero. This is a single value that we will use in our analysis to divide acceptable positive stability from unacceptable negative stability.

Negative stability is then when there is an upward force at the right wheel. This will result in our entire system of passengers and car rotating counterclockwise around the pivot point until

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stopped by some other limitation (such as the frame hitting the ground). This is the stability result we want to avoid..

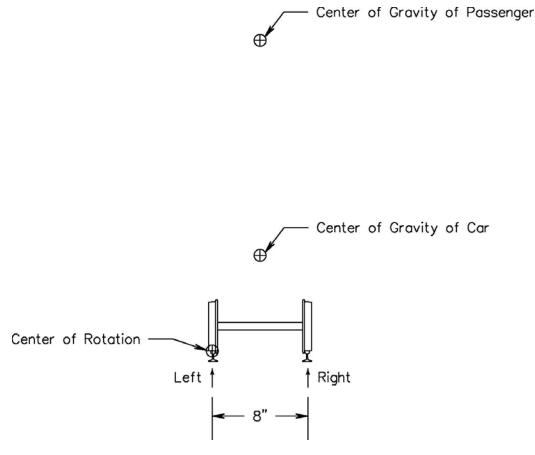


Figure 1 – Basis of Analysis

### **Moments and Forces**

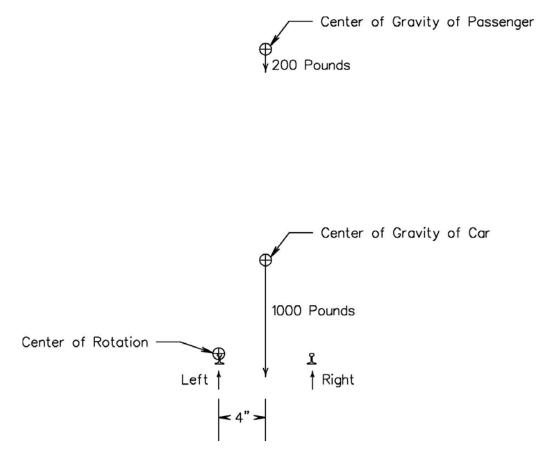
The analysis used for most of this report is based on the engineering science of statics. In this we are considering forces that are unchanging (static) during the analysis. In a complete analysis we would consider linear forces (up and down) and rotational (turning) forces. For our analysis here we need only consider these rotational forces as a torque. The unit of torque we will use is the inch-pound which is defined as a force of one pound operating on a moment arm of one inch. In all cases we are simply using a weight in pounds as the force.

Since the left side wheel to rail contact point is our pivot point we will analyze rotary moments about this point. In order to show the difficulty of obtaining stability we have decided to use weights that in many cases are much larger than typically found in this size of equipment. In all of the following analysis we will use a weight of 1000 pounds for an empty car. We will then

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also use a weight of 200 pounds for the passenger that is the focus of this analysis, that is, someone that causes a stability problem.

We can now redraw the initial figure in a more typical engineering way as shown in Figure 2. We show the weights as downward pointing arrows and we have made the length of the arrows proportional to the amount of weight.



**Figure 2 – Adding Weights Define Forces** 

In a conventional analysis this figure, plus the horizontal and vertical dimensions to each of the forces would be analyzed as shown in Figure 3. It is necessary to calculate the length of each moment arm along its diagonal. It is also necessary to break the force from the weight into its component part that is perpendicular to the moment arm. This analysis requires considerable math and yields the same result of a simplified method discussed in the next section.

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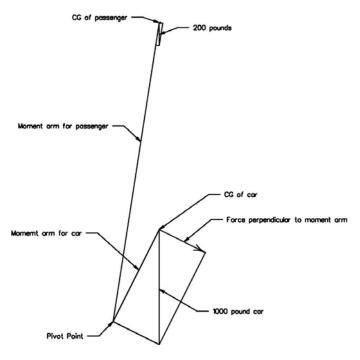


Figure 3 – Conventional Statics Analysis

#### Analysis in One Dimension

To simplify our analysis we can eliminate the vertical information and consider only the forces and their horizontal positioning as shown in Figure 4. If we were doing a complete analysis and wanted to know the vertical and horizontal forces at every point, including the pivot point, we could not make this simplification.

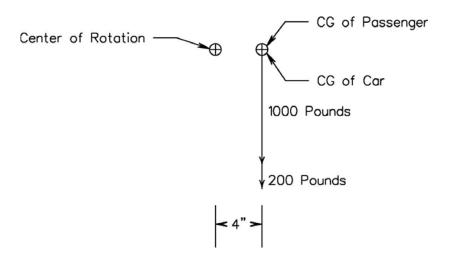


Figure 4 – One Dimensional Simplified Analysis – Case #1

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Since we now have the center of gravity (CG) of the car and passenger at the same point we can now simply add their force arrows by drawing them end to end.

## **Stability Analysis Test Cases**

Having established a lot of background we can now look at specific cases of stability, starting with the one already partially developed.

### Stability Case #1

This analysis is based on a 1000 pound car, centered over its wheels, and a 200 pound passenger, also in the center of the car as previously shown in Figure 4.

From this we can calculate a torque of:

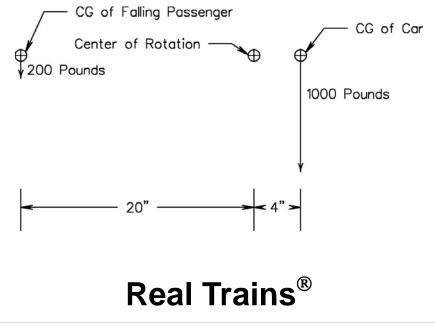
(1000 pounds + 200 pounds)(4 inches) = 4800 inch pounds clockwise

This large clockwise value is resisted by the force of the right side wheel against the right side rail. This is a very stable situation.

### Stability Case #2

Now let us assume that the one passenger weighing 200 pounds begins to fall out of the car to the left side. The reason for this falling does not matter but what is very important is that the person remains in contact with the car. What this means is that the person is holding on to the car and will transfer any torques resulting from their change in position to the overall system including the car and other passengers.

In this analysis we move the center of gravity of the falling person 20 inches to the left of the pivot point as shown in Figure 5. This number is arbitrary and was selected to make the math simpler.



#### Figure 5 – Stability Case #2 – Falling Passenger

The clockwise torques are:

(1000 pounds)(4 inches) = 4000 inch pounds

And counterclockwise torques are:

(200 pounds)(20 inches) = 4000 inch pounds

The two values are equal and, consequently, offset each other. This results in there being no weight on the right side wheels. The car may not have started to overturn yet but the slightest force will cause it to not only start to turn but to continue until stopped by something outside of our analysis such as contact with the ground.

#### Back to Two Dimensions

In the preceding analysis we have considered the location of a force only as to its horizontal position. This analysis is simpler and accurate for our needs. There is, however, a need to at least talk about the effect of the vertical positions of the forces.

The neutral stability case is a convenient dividing point between stable and unstable results. It, however, is not really a position that a real system would remain in for very long. The reason for this is that the CG's of the passenger and the car are above (in the two dimensional world) the pivot point. Starting at the neutral stability point the slightest rotation of the system (car and passenger) counterclockwise will have the effect of moving the falling passenger CG farther to the left, away from he pivot point. This increases the effect of the passenger weight and decreases the opposing effect of the car weight and results in a increasingly rapid rate of rotation.

For these reasons the configuration of Case #2 is very unstable. It should be noted here that a single passenger of reasonable size can turn over even an extremely heavy car.

### Stability Case #3

In looking at what we have done so far it normal to assume that a car would have more than one passenger. For this next case we will add two additional passenger, each of 250 pounds and have them sit in the center of the car. This is shown in Figure 6.

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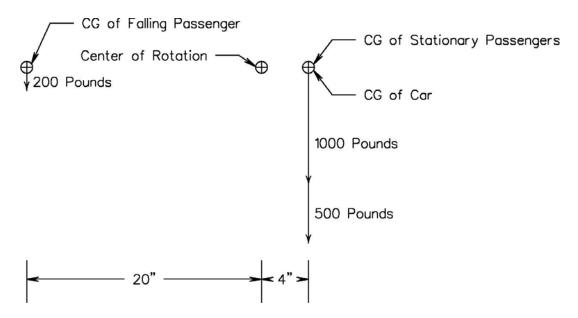


Figure 6 – Stability Case #3 – Additional Passengers in Center

The clockwise torques are:

(1000 pounds + 500 pounds)(4 inches) = 6000 inch pounds

And counterclockwise torques are:

(200 pounds)(20 inches) = 4000 inch pounds

From this we see that the car in now very stable again. We could actually have added any amount in the form of passengers or a heavier car and gotten the same results.

### Stability Case #4

When considering the falling passenger we can develop a number of reasons for the person actually falling. This report does not intend to go into this subject but some ideas are presented in the summary section that are relative to this.

It is reasonable to assume that in some cases whatever made the falling person move may also effect the other passengers. Even at the limited speeds we operate at a large structure such as a bridge can appear suddenly enough to surprise a new rider. For this next analysis case we will assume that whatever made one person fall also caused the other two passengers to move somewhat to the same side. Other than this the case is the same as the previous case and is shown in Figure 7.

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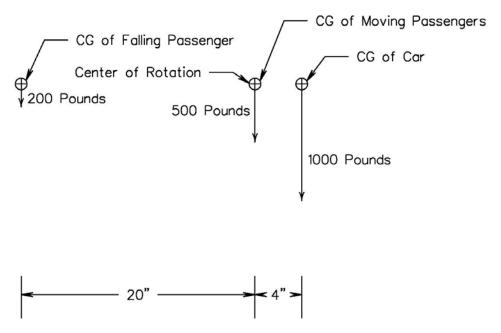


Figure 7 – Stability Case #4 – Added Passengers Also Moving

For the purposes of this analysis we have moved both of the added passengers four inches to the left. As you can see this positions them directly over the center of rotation and this results in their weight having no effect since the moment arm is now zero inches (and the weight times zero is zero). This gives us the same answer as case #2:

The clockwise torques are:

(1000 pounds)(4 inches) = 4000 inch pounds

And counterclockwise torques are:

(200 pounds)(20 inches) = 4000 inch pounds

And we are again ready to turn the car over.

You can, of course, speculate that the persons may move three or five inches and may help or hurt stability. The configuration selected was done to illustrate that weight without a moment arm does not help stability.

### Conclusions

From the information presented we can see that it is very difficult to assure stability in the operation of a 7 1/2" gauge train. It is assumed that the persons operating the train will do everything possible to prevent persons from being put into the situation where they are capable

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of turning over a train. Being a stationmaster is a difficult enough job without have to impose the additional requirements of telling some persons that they cannot be given a ride. A similar problem exists once the train is under way for a conductor that is required to stop the train and remove a rider that is acting in an unsafe way. But even with these steps a sudden, unexpected movement by one person can turn over even the best constructed and managed train.

There is, however a possible solution. If you remember that in starting this analysis we made the assumption that the falling person acted as part of the system, transferring their forces to the car and other passengers. If we change this such that the falling person is unable to hold on to the car, they would then still fall but would not take the rest of the system with them.

While this sounds undesirable, and is certain to be both controversial and something that many persons will not want widely publicized, designing a car so someone will fall off is actually the only way to insure the safety of the other passengers. We are all certain that we never want to see someone injured but this analysis supports the fact that we must isolate the person from the car.

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